

# CLASS 12 PHYSICS — FORMULA SHEET

Chapter 13 : Nuclei (NCERT)

## 13.1 Nucleus — Composition & Size

| Concept                       | Formula / Detail                                                             |
|-------------------------------|------------------------------------------------------------------------------|
| Notation                      | ${}^A_ZX$ : A = mass number, Z = atomic number, N = A – Z neutrons           |
| Nuclear radius                | $R = R_0 A^{1/3}$ ; $R_0 = 1.2 \times 10^{-15}$ m (fermi)                    |
| Nuclear volume                | $V \propto A$ (proportional to mass number)                                  |
| Nuclear density               | Nearly constant ( $2.3 \times 10^{17}$ kg/m <sup>3</sup> ), independent of A |
| Atomic mass unit (u)          | 1 u = $1.66 \times 10^{-27}$ kg = 931.5 MeV/c <sup>2</sup>                   |
| Isotopes / isobars / isotones | Same Z / same A / same N                                                     |

## 13.2 Mass–Energy & Binding Energy

| Concept                    | Formula                                                                       |
|----------------------------|-------------------------------------------------------------------------------|
| Einstein mass–energy       | $E = mc^2$ ; 1 u = 931.5 MeV                                                  |
| Mass defect                | $\Delta m = [Z m_p + (A-Z) m_n] - M_{\text{nucleus}}$                         |
| Binding energy             | $BE = \Delta m \times c^2 = \Delta m \text{ (in u)} \times 931.5 \text{ MeV}$ |
| Binding energy per nucleon | $BE/A = BE \div A$ (measure of stability)                                     |
| Most stable nuclei         | Around $A \approx 56$ (iron) ; $BE/A \approx 8.8$ MeV (maximum)               |
| Heavy & light nuclei       | Lower $BE/A \rightarrow$ less stable $\rightarrow$ undergo fission/fusion     |

## 13.3 Radioactivity & Decay Law

| Concept               | Formula                                                                    |
|-----------------------|----------------------------------------------------------------------------|
| Radioactive decay law | $N = N_0 e^{(-\lambda t)}$ ( $\lambda$ = decay constant)                   |
| Activity              | $A = \lambda N = A_0 e^{(-\lambda t)}$ ; unit becquerel (Bq) or curie (Ci) |
| Half-life             | $T_{1/2} = 0.693 \div \lambda = (\ln 2) \div \lambda$                      |
| Mean (average) life   | $\tau = 1 \div \lambda = T_{1/2} \div 0.693 = 1.44 T_{1/2}$                |
| After n half-lives    | $N = N_0 \div 2^n$ ; $n = t \div T_{1/2}$                                  |
| 1 curie               | 1 Ci = $3.7 \times 10^{10}$ Bq (decays/sec)                                |

## 13.4 Types of Radioactive Decay

| Decay                          | Equation & Detail                                                                            |
|--------------------------------|----------------------------------------------------------------------------------------------|
| Alpha ( $\alpha$ ) decay       | ${}^A_ZX \rightarrow ({}^{A-4}_{Z-2})Y + {}^4_2\text{He}$ ; $A \downarrow 4, Z \downarrow 2$ |
| Beta-minus ( $\beta^-$ ) decay | ${}^A_ZX \rightarrow {}^A_{(Z+1)}Y + e^- + \bar{\nu}$ ; neutron $\rightarrow$ proton         |
| Beta-plus ( $\beta^+$ ) decay  | ${}^A_ZX \rightarrow {}^A_{(Z-1)}Y + e^+ + \nu$ ; proton $\rightarrow$ neutron               |
| Gamma ( $\gamma$ ) decay       | Excited nucleus $\rightarrow$ ground state + $\gamma$ photon ; A & Z unchanged               |

| Decay             | Equation & Detail         |
|-------------------|---------------------------|
| Penetrating power | $\gamma > \beta > \alpha$ |
| Ionising power    | $\alpha > \beta > \gamma$ |

### 13.5 Nuclear Fission & Fusion

| Concept                | Detail                                                                                                      |
|------------------------|-------------------------------------------------------------------------------------------------------------|
| Nuclear fission        | Heavy nucleus splits into lighter nuclei + energy (e.g. U-235)                                              |
| Fission example        | ${}^{235}_{92}\text{U} + n \rightarrow {}^{141}_{56}\text{Ba} + {}^{92}_{36}\text{Kr} + 3n + \text{energy}$ |
| Energy per fission     | 200 MeV                                                                                                     |
| Chain reaction         | Released neutrons trigger further fissions                                                                  |
| Nuclear fusion         | Light nuclei combine into a heavier one + energy                                                            |
| Fusion example         | Hydrogen $\rightarrow$ helium (powers the Sun)                                                              |
| Why energy is released | Products have higher BE/A $\rightarrow$ mass converted to energy                                            |
| Conditions for fusion  | Very high temperature & pressure (thermonuclear)                                                            |

### ★ QUICK MEMORY AIDS & TRICKS

|                           |                                                                                                    |
|---------------------------|----------------------------------------------------------------------------------------------------|
| Nuclear radius            | $R = R_0 \times A$ raised to $1/3$ . Density is the SAME for all nuclei (independent of A).        |
| 1 u = 931.5 MeV           | Convert mass defect (in u) to energy by multiplying by 931.5 MeV.                                  |
| Binding energy            | $BE = \Delta m \times 931.5 \text{ MeV}$ . Higher BE/A $\rightarrow$ more stable nucleus.          |
| Most stable               | Iron (A about 56) has the highest BE/A, about 8.8 MeV.                                             |
| Half-life                 | $T_{1/2} = 0.693/\lambda$ ; mean life $\tau = 1/\lambda = 1.44 T_{1/2}$ .                          |
| n half-lives              | $N = N_0/2^n$ . After 3 half-lives, 1/8 remains.                                                   |
| Penetration vs ionisation | Penetration: $\gamma > \beta > \alpha$ . Ionisation: $\alpha > \beta > \gamma$ (exactly reversed). |
| Fission vs fusion         | Both release energy by moving toward higher BE/A (iron peak).                                      |